

CSCI 313 Data Structure

Midterm 1 - B

First Name: _____

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1. **ArrayQueue** is defined as following(12 points):

```
Class ArrayQueue<E> implements Queue<E>, Iterable<E>{
    private int capacity =10;
    private E[] elements = (E[]) new Object[capacity];
    private int size;
    private int first;
    private int last;
    //methods we implemented in class.
    public Iterator<E> iterator(){
        return new QueueIterator();
    }
    //Implement its iterator class for ArrayQueue
    private class QueueIterator implements Iterator<E>{
        //you may declare variables here.

        private int index = first

        public QueueIterator(){

        }

        public Boolean hasNext(){
            return index!= last;
        }

        public E next(){

            E val = elements[index++];
            if(index == capacity){
                index = 0;
            }
            return val;
        }

        public void remove(){
            throw new UnsupportedOperationException();
        }
    }
}
```

2. Estimate the runtime using Big-O (**8 points**):

a) What's the runtime of **hasNext()** and **next()** method in Q1.

$O(1)$

b) $T(n) = 10\log_2(n^2) + 15\log_2((2n)^2) + 5\log_2(n^5) + 200\log_2(1000^5)^2 + 10000$

$O(\lg n)$

c) $T(n) = 60T(n/2) + 10n^4$

$a = 60, b = 2, d = 4$

$O(n^{\log_2 60})$

d) $T(n) = 9T(n/3) + 100n^2$

$O(n^2 \log_3 n)$

e) $T(n) = 63(n/4) + 3n^3$

$O(n^3)$

$$f) T(n) = 2T(n - 3) + 1$$

Assume $n = k * 3 + 1$, k is 1,2,3,4,5,6.....

$$T(n - 3) = 2T(n - 6) + 1$$

$$T(n - 6) = 2T(n - 9) + 1$$

$$T(1) = 1$$

$$T(n) = 2T(n - 3) + 1 = 2^2T(n - 6) + 2 + 1$$

$$= 2^k T(1) + 2^{k-1} + \dots + 2 + 1$$

$$= O(2^{n/3})$$

3. Remove Last element in Queue(5 points)

Define a method to remove the last element of queue. Other elements remains the same order.

You can only invoke enqueue(), dequeue(), size(), isEmpty(), peek() methods. You should NOT declare any datastructures. 0 points if you have more than 10 lines code.

Ex1:

```
Queue<Integer> s = new Queue<>();
```

```
//push 1 2 3 4 5 into queue.
```

```
removeLast(s): return 5
```

```
removeLast(s): return 4
```

```
removeLast(s): return 3
```

```
public E removeLast(Queue<E> queue){  
    for(int i= 1;i<size;i++){  
        queue.enqueue(queue.dequeue());  
    }  
    return queue.dequeue();  
}
```

```
}
```